# Modeling of a Three Legged Self Supporting Telecommunication mast under sudden side wind Crash Loading 

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#### Abstract

This Paper is on the modeling of telecommunication mast in a windy environment. The effect of sudden side crash wind load on a 3-legged Self Supporting Telecommunication Mast was studied in a 3-D modeling ANSYS environment. The behavioral patterns under full loading in windy environment were observed. The full loading being the self weight, communication system weight coupled with wind load. The effects of the bolts were neglected. The height of the modeled mast is $26.58 \mathrm{~m}(2658 \mathrm{~cm}$ or 26580 mm$)$. The mast was subjected to wind load from the side at different heights with the top mast having a load of 6196 N and 12908 N at height 8.36 m , in addition to the system load. A displacement of 17.486 mm was seen to occur at the top and 0 mm at the base showing a fatigue loading at wind frequencies. The fatigue loads were observed to be much below the fatigue limit (endurance limit for mild steel). Direct stresses showed compressive stresses concentrated on a leg and of greater magnitude than tensile stresses developed on each of the two other legs opposite the points of wind application. The tensile stresses were balanced out by the compressive stresses to maintain mast stability.


Index Terms- Telecommunication mast, Deformation, Stress analysis, Wind load, ANSYS, Fatigue, Modeling.

## 1 INTRODUCTION

A Self Supporting Telecommunication mast serves as a medium for receiving and transmitting wireless type of communication which includes mobile and internet net work, television and radio broadcasting and also integration of radar system. Generally, the masts are tapered upwards and usually supported at several levels along its height by a set of varying angle bracing member. The members are designed either as compression or tension members. This is because failure of any member will lead to the total failure of the structure. Failure originates from the kinds of loading the mast is subjected to such as (self weight or weight of antenna etc) and dynamic loading i.e. wind strike that is associated with altitude.(Mohd et al.,2013) [2]

A self supporting telecommunication mast has a larger foot print than monopole, but still requires a much smaller area than guyed mast. Due to its relatively small foot print, this kind of mast is commonly seen in cities or other places where it is short of free space. They free stand with three or four legs connected by a lattice work braces. Self supporting telecommunication masts can utilize a single foundation supporting all the legs or individual foundations below each leg. Due to the loading lattice mast foundations can experience both vertical and horizontal loads. The vertical loads act in both the upwards and downwards direction as the mast attempts to overturn. The horizontal or shear loading can act in any direction as the direction of the wind can vary. (http://www.cdc.gov) , (Stottrup, 2012) [5]

For some years, the finite element method has been applied to solve the solid mechanics problems in view of its accuracy, convenience and flexibility.2-D modeling is known for its simplicity and ability to run on normal computer. This research attempt to simulate and analyze the deformation and stress distribution on a 3-D modeling of a telecommunication mast employing finite element method by the means of
commercial soft ware known as ANSYS 14.0 as the modeler and processor. The study is significant in structure material selection and design process prior to fabrication and installation. By using ANSYS, failure behavior of the structure is simplified and there is a reduction or elimination of physical tests.

## 2 MODELING PROCEDURES

The overall procedure consist of (i) 3D Modeling of 3-legged self supporting telecommunication mast with $L$ cross section (ii) Stress analysis of the masts (iii) Deformation of the mast under the action of wind load which are made to strike the mast from a particular direction, with all other loads in consideration and (iv) Analyzing the stresses and deformation on the Modeled Telecommunication Mast.

### 2.1 The Governing Equations and boundary conditions

Figure 1 shows a three dimensional truss in space. The governing equations are expressed in equation 1.


Fig .1. A bar in a 3-D Truss (space truss ) (Survranu ,2002)

$$
K=\mathrm{EA} / \mathrm{L}\left[\begin{array}{cccccc}
l_{1}{ }^{2} & l_{1} m_{1} & l_{1 n_{1}} & -l_{1^{2}} & -l_{1} m_{1} & -l_{1 n_{1}}  \tag{1}\\
l_{1 m_{1}} & m_{1^{2}} & m_{1 n_{1}} & -l_{1} m_{1} & -m_{1^{2}} & -m_{1 n_{1}} \\
l_{1 n_{1}} & m_{1 n_{1}} & n_{1^{2}} & -l_{1 n_{1}} & -m_{1 n_{1}} & -n_{1^{2}} \\
-l_{1^{2}} & -l_{1 m_{1}} & -l_{1 n_{1}} & l_{1^{2}} & l_{1 m_{1}} & l_{1 n_{1}} \\
-l_{1 m_{1}} & -m_{1^{2}} & -m_{1 n_{1}} & l_{1 m_{1}} & m_{1^{2}} & m_{1 n_{1}} \\
-l_{1 n_{1}} & -m_{1 n_{1}} & -n_{1}{ }^{2} & l_{1 n_{1}} & m_{1 n_{1}} & n_{1}{ }^{2}
\end{array}\right]
$$

Where K is the element stiffness matrix in the global coordinate, A is the area of cross section of the bar; L is the length of the bar.
$\mathrm{l}_{1}, \mathrm{~m}_{1}$ and $\mathrm{n}_{1}$ are the direction cosines of $\hat{x}$
$\mathrm{l}_{1}=\operatorname{Cos} \theta_{\mathrm{x}}, \mathrm{m}_{1}=\operatorname{Cos} \theta_{\mathrm{y}}, \mathrm{n}_{1}=\operatorname{Cos} \theta_{\mathrm{z}}$

$$
\begin{equation*}
\mathrm{F}=\mathrm{KU} \tag{2}
\end{equation*}
$$

Where F is the Load vector of the truss element and d is the displacement (Survranu , 2002) [6]. Figure 1 shows the displacement that occurs in each of the mast element. The displacement $u(x, y, z)$ at the feet of the mast satisfies the simple dirichlet boundary condition i.e. $u(x)=0, u(y)=0, u(z)=0$. Dirichlet may also be known as fixed or essential boundary condition.

### 2.2 Basic steps in the modeling of the telecommunication mast



The views of some of the modeling steps are show in figure ( $2,3,5$ and 6 )

TABLE 1

| Material Properties | Values |
| :--- | :--- |
| Young's Modulus | 210 GPa |
| Coefficient of Thermal Expansion | $1.2 \times 10^{-5} \mathrm{C}^{0-1}$ |
| Tensile Strength | 4.99 GPa |
| Yield Strength | 3.57 GPa |
| Density | $7861 \mathrm{~kg} / \mathrm{m}^{3}$ |
| Temperature | $27^{\circ} \mathrm{C}$ |



Fig. 2. Isometric view of Generated line bodies


Fig. 3. Isometric view of mast with cross section


Fig. 4. Material (Angle Bars) Type.(Mohd et al.,2013) [2]

TABLE 2
PARAMETERS OF THE BARS

| Members | Width | Thickness | Angle, Mass \& volume |
| :--- | :--- | :---: | :---: |
| Foot | 400 mm | 100 mm | $90^{\circ}$ |
| Brace and Joint | 150 mm | 20 mm | $90^{\circ}$ |
| Mass and Volume of  <br> the structure  | $13008 \mathrm{~kg}, 1.6571 \mathrm{e}+009$ | $\mathrm{~mm}^{3}$ |  |



Fig. 5. Isometric view of meshed mast


Fig.6. Setting up joint connection (isometric view)

### 2.3 Obtaining value of forces on various height of the mast

Several values of the wind forces for various height and area are shown in table 3 below. The graph is figure 3 show that as the height of the mast increases, the values of the wind load decreases. The values of the wind load were calculated using equation (3). The wind speed was assumed to be $45 \mathrm{~m} / \mathrm{s}$. This was kept constant all through the heights, acting at an elevation of 8.36 m above the ground, so was the density of the wind. Area is simply the area of the face the sudden wind strikes i.e. the face perpendicular to the wind force. It is obvious from table 3 that as the height of the mast increase, the areas of the element increase, this actually prompted increase in the wind the values of the wind forces. In figure 8 below, the load acts perpendicular on one side of the mast while the system loads $(2400 \mathrm{~N})$ act down wards.

$$
\begin{equation*}
\mathrm{Fw}_{\mathrm{w}}=1 / 2\left[\mathrm{C}_{\mathrm{d}} \cdot \mathrm{~V}^{2} . \text { A. } \mathrm{Q}\right](\text { Rajan, 2013 })[4] \text {, Pahwa et.al [3] } \tag{3}
\end{equation*}
$$

$F_{W}=$ Force due to wind (N), $Q=$ Air density $\left(1.22 \mathrm{~kg} / \mathrm{m}^{3}\right), C_{d}=$ Drag coefficient (from text or experimental data), $\mathrm{V}=$ Wind velocity ( $\mathrm{m} / \mathrm{s}$ ), $\mathrm{A}=$ Cross sectional area perpendicular or normal to wind direction (e.g. length * width). The figures below shows drag coefficient for various profile. $\mathrm{C}_{\mathrm{d}}$ for a rectangular profile is 1.9 (Rajan, 2013) [4]

TABLE 3
CALCULATING VALUES OF WIND LOAD

| $\mathrm{H}(\mathrm{m})$ | $\mathrm{V}(\mathrm{m} / \mathrm{s})$ | $\mathrm{P}\left(\mathrm{kg} / \mathrm{m}^{3}\right)$ | $\mathrm{Cd} \quad \mathrm{A}\left(\mathrm{m}^{2}\right)$ | $\mathrm{Fw}(\mathrm{N})$ |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| 08.36 | 45 | 1.22 | 1.9 | 5.50 | 12908 |
| 11.36 | 45 | 1.22 | 1.9 | 4.95 | 11618 |
| 14.21 | 45 | 1.22 | 1.9 | 4.50 | 10561 |
| 16.86 | 45 | 1.22 | 1.9 | 4.10 | 9623 |
| 19.46 | 45 | 1.22 | 1.9 | 3.71 | 8707 |
| 21.94 | 45 | 1.22 | 1.9 | 3.33 | 7815 |
| 24.29 | 45 | 1.22 | 1.9 | 3.00 | 7041 |
| 26.58 | 45 | 1.22 | 1.9 | 2.64 | 6196 |



Fig.7. Graph of Mast height against the Wind load


Fig. 8. Application of loads and other constraints


Fig. 9. Side view showing application of Loads


Fig. 10. Top view showing application of Loads

## 3 RESULTS AND DISCUSSION

As a result of the external applied forces (wind load) and the system loads on the modeled mast, it undergoes deformation as shown in fig 11 . The mast resists the force. Total displacement and directional
displacement were solved for. The total displacement as shown in fig 11 is the vector sum of the directional displacements. It was maximum at the extreme top of the mast even though the wind load applied to that region was lower. The top offered less resistance because of the smaller area. Total displacement decreased down the mast and was minimum at the foot of the mast.

Direct stresses acted perpendicular to the cross section of the mast's body or the elements. As shown in figure 12 , the value of the maximum direct tensile stress on each of the mast foot where the wind load impacted was 33.818 MPa and the value of the maximum direct compressive stress on the third foot of the mast was -68.569 MPa showing a balance of forces. The force on the third foot being higher shows higher stress level for fatigue. However, the fatigue limit for mild steel undergoing compression-tension is 250MPA (Mayer and Stanzl-Tschegg, 2015) [1] which shows that the compressive forces are far below the fatigue limit. However, it has been proved that after a long time these stresses still have debilitating effect on the structure (Mayer and Stanzl-Tschegg, 2015) [1]


Fig. 11. Results of the total deformation


Fig. 12. Direct stress on the Modeled Mast
The value of the maximum displacement was 17.486 mm , it decreases down the mast, and the minimum was 0 . The value of the maximum stress was 33.818 MPa (Tensile) it also decreases down the mast and the minimum value was - 68.569 MPa (Compressive).

## 4 CONCLUSION

Telecommunication Mast of height 26.58 m ( 2628 cm ) was modeled and simulated using ANSYS 14.0.The value of the maximum total displacement is 17.486 mm i.e. $(1.7486 \mathrm{~cm}$ or 0.017486 m$)$ within a second of sudden load wind strike. Deformation and displacement is minimal towards the base of the mast; it is zero at the base of the mast. This is due to the large area at the base and the fixed support at the base. The less number of structural members at the foot also affects its rigidity. The higher a telecommunication mast length, the more tapered it is at the top and the more likely it is to have higher displacement at the top. Direct stresses (Compressive and Tensile) are highest at the foot. Masts contain rigid truss elements which may not collapse when loaded but may only deform slightly, but cycles of deformation loads will eventually weaken the mast. From this modeled mast it can be concluded that the mast will withstand those values of sudden wind loads strikes not taking into consideration long -term corrosion effects on the structural members.

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